

7.3: Use Functions involving "e"

e → Natural base

e is found using the expression:

$$\left(1 + \frac{1}{n}\right)^n$$

by plugging in various numbers we can approximate e

$$1 \rightarrow \left(1 + \frac{1}{1}\right)^1$$

$$\frac{(1+1)^1}{2^1} = 2$$

$$2 \rightarrow \left(1 + \frac{1}{2}\right)^2$$

$$\left(\frac{3}{2}\right)^2 = 2.25$$

⋮

$$10 \rightarrow \left(1 + \frac{1}{10}\right)^{10} = 2.59374$$

$$100 \rightarrow \left(1 + \frac{1}{100}\right)^{100} = 2.70481 \approx 2.7$$

$$1000 \rightarrow \left(1 + \frac{1}{1000}\right)^{1000} = 2.71692 \approx 2.71$$

$$10000 \rightarrow \left(1 + \frac{1}{10000}\right)^{10000} = 2.71815 \approx 2.718$$

$$100000 \rightarrow \left(1 + \frac{1}{100000}\right)^{100000} = 2.71827 \approx 2.7182$$

so, as $e \rightarrow \infty$ (e approaches infinity)

$$e \approx 2.71828$$

$$e^0 = 1$$

$$e^1 = 2.718$$

example 1: Simplify

a. $e^7 \cdot e^4 = e^{11}$

b. $\underline{2e^{-3}} \cdot \underline{6e^5} = 12e^2$

c. $\frac{24e^8}{4e^5} = 6e^3$

$$d. (10e^{-4x})^3$$

$$10^3 e^{-4x \cdot 3}$$

$$1000 e^{-12x}$$

$$e) \sqrt[3]{8e^{6x}}$$

$$2e^{2x}$$

$$\begin{array}{r} 2 \overline{) 8} \\ \underline{4} \\ 2 \overline{) 4} \\ \underline{2} \\ 2 \overline{) 2} \\ \underline{2} \\ 0 \end{array}$$

$$e^x e^x e^x \quad e^x e^x e^x$$

***works just like last semester:

$$\sqrt[3]{x^5} \quad \begin{array}{c} \text{XXXXXX} \\ \downarrow \\ x \sqrt{x^2} \end{array}$$

Example 2: use a calculator to evaluate

a. $e^{3/4} \approx 2.117$

b. $e^{-.28} \approx .7558$

②

Graphing e

Standard Form:

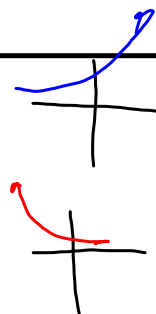
$$y = a \cdot e^{r(x-h)} + k$$

$$b = e^r$$

y-intercept: (0, a)

2nd point: (1, ab)

If r is positive it is an exponential growth
If r is negative it is an exponential decay



Example 3: Graph

$$\text{a. } y = 4e^{0.5x}$$

$a = 4$ $b = e^{0.5}$
 $b \approx 1.6$

Pts:

$$(0, 4)$$

$$(1, 6.4)$$

Shift:

None

Asymptote:

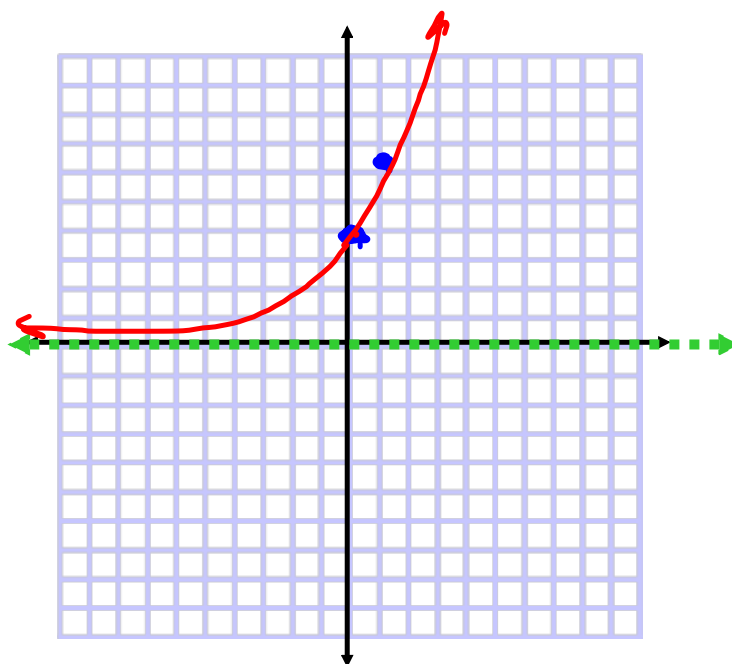
$$y = 0$$

Domain:

$$(-\infty, \infty)$$

Range:

$$(0, \infty)$$



$$c. \ y = e^{-1.5(x-2)} - 4$$

$$a = 1 \quad b = e^{-1.5}$$

$$b \approx .22$$

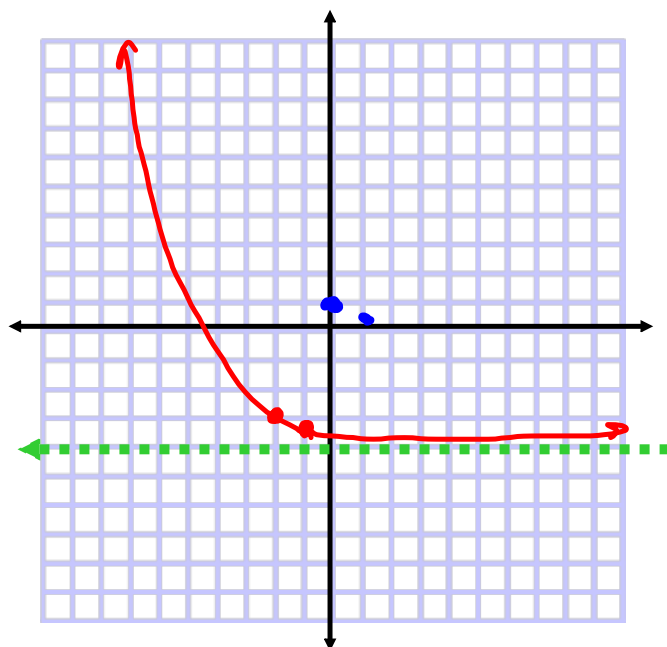
Pts: $(0, 1)$
 $(1, .22)$

Shift: Left 2 Down 4

Asymptote: $y = -4$

Domain: $(-\infty, \infty)$

Range: $(-4, \infty)$



Continuously Compounded
Interest

$$A = Pe^{rt}$$

P = initial amount

r = %

t = years

Example:

You deposit \$3,000 into an account that pays 3.5% annual interest compounded continuously. What is the balance after 3 years.

$$A = P e^{rt}$$

$$P = 3000$$

$$r = .035$$

$$t = 3$$

$$3000 e^{.035(3)}$$

$$3000 e^{.105}$$

$$3000 (1.11)$$

$$\$ 3330.00$$